LatFit - Producing high accuracy lattice models from protein atomic co-ordinates including side chains

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Abstract

Background: Lattice models are a common abstraction used in the study of protein structures and related topics. Various approaches to the *protein chain lattice fitting* problem have been suggested but only one tool is currently openly available and this is for backbone-only models.

Results: We introduce LatFit, a new tool to produce high accuracy lattice protein models from protein atomic co-ordinates. It generates backbone-only models as well as lattice models including side chains in various lattice types. LatFit implements a new dRMSD-optimisation fitting procedure in addition to a known cRMSD-optimising method. The program is freely available for download or as a web server at http://cpsp.informatik.uni-freiburg. de

Conclusions: We model a large non-redundant set of high resolution proteins (SCOP database) on three commonly used lattices: 3D cubic (100), face centred cubic (FCC, 110), and knight's walk (210). Both backbone and side chain models produced by LatFit show low deviation from the original data (e.g. 1.5Å RMSD in FCC lattice). To our knowledge, this is the first comprehensive study of lattice quality for on-lattice protein models including side chains.

Background

It is not always computationally feasible to undertake protein structure studies using full atom representations. The challenge is to reduce complexity while maintaining detail [1–3]. Lattice protein models are often used to achieve this but in general only the protein backbone or the amino acid centre of mass is represented [4–11]. A huge variety of lattices and energy functions have previously been developed [4, 12, 13].

In order to evaluate the applicability of different lattices and to enable the transformation of real protein structures into lattice models, a representative lattice protein structure has to be calculated. Maňuch and Gaur have shown the NP-completeness of this problem for backbone-only models in the 3Dcubic lattice and named it the *protein chain lattice fitting (PCLF) problem* [14].

The PCLF problem has been widely studied for

backbone-only models [12, 15–22]. The most important aspects in producing lattice protein models with a low root mean squared deviation (RMSD) are the lattice co-ordination number and the neighbourhood vector angles [17,22]. Lattices with intermediate coordination numbers, such as the face-centred cubic (FCC) lattice, can produce high resolution backbone models [17] and have been used in many protein structure studies (e.g. [3, 23, 24]). However, the use of backbone models is limited since they do not account for the space required for side chain packing.

To overcome this restriction lattice protein models that include side chains have been introduced [25–31]. Reva *et al.* have to our knowledge developed the only approach to solve the PCLF problem [30]. The CABS-tools by Kolinski and coworkers utilize a hybrid on-lattice (backbone) and off-lattice (side chain) protein representation does not attempt to answer the PCLF problem [29, 32].

In this manuscript we use the side chain model definition of Bromberg and Dill [26], where each amino acid is represented by two on-lattice monomers: one represents the side chain atoms and one the C_{α} atom. This explicit representation of side chains prevents unnatural collapse during structural studies [33] and enables the reconstruction of full atom protein data [34].

To the best of our knowledge, there is only one publicly available approach, namely LocalMove, to derive lattice protein models from real proteins despite a large number of published methods. LocalMove was introduced by Ponty *et al.* for backbone-only models in 3D-cubic and FCC lattice [21].

We present our tool LatFit to tackle this lack of available implementations. LatFit solves the PCLF problem, i.e. transforms a protein from full atom co-ordinate data to a lattice model, and is available as both a stand-aloneone tool for high-throughput pipelines and a web interface for *ad hoc* usage. A new fitting procedure that optimises distance RMSD enables rotation independent lattice model creation of protein structures. The method is applicable to arbitrary lattices and handles both backbone and side chain representations with equivalent accuracy. A depiction of the workflow is given in Fig. 1.

Utilising LatFit we present the first comprehensive study of lattice quality for protein models including side chains. In our test, LatFit fitted the majority of models on an FCC lattice within $1.5\mathring{A}$ RMSD.

Methods

In order to enable a precise formulation of the method we introduce some prelimary definitions. A lattice L is defined by a set of neighboring vectors $\vec{n} \in N$ of equal length $(\forall_{\vec{n_i},\vec{n_j} \in N} : |\vec{n_i}| = |\vec{n_j}|),$ each with a reverse $(\forall_{\vec{n}\in N} : -\vec{n} \in N)$, such that $L = \{ \vec{x} \mid \vec{x} = \sum_{\vec{n}_i \in N} d_i \cdot \vec{n}_i \wedge d_i \in \mathbb{Z}_0^+ \}. \ |N| \text{ gives the}$ coordinate number of the lattice, e.g. 6 for 3D-cubic or 12 for the FCC lattice. A lattice protein structure with side chains of length l is defined by a sequence of lattice nodes $M^b = (M_1^b, \dots, M_l^b) \in L^l$ representing the backbone monomers of each amino acid and the according sequence $M^s = (M_1^s, \ldots, M_l^s) \in L^l$ for their side chain position. A valid structure ensures backbone connectivity $(\forall_{i < l} : M_i^b - M_{i+1}^b \in N)$, side chain connectivity $(\forall_i : M_i^b - M_i^s \in N)$, as well as selfavoidance $(\forall_{i\neq j}: M_i^b \neq M_j^b \land M_i^s \neq M_j^s$ and $\forall_{i,j} : M_i^b \neq M_j^s).$

Fitting Procedure

Given a protein structure of length l in Protein Database (PDB) format [35], LatFit builds up the lattice protein sequentially, one amino acid at a time, starting from the amino-terminus.

First, all neighboring vectors $\vec{n} \in N$ of the used lattice L are scaled to a length of $3.8 \mathring{A}$, which is the mean distance between consecutive C_{α} atoms and close to the mean distance between a C_{α} atom and the associated side chain centroid ($\approx 3.6 \mathring{A}$). This scaling enables a reasonable mapping of the protein into the lattice; since each amino acid will be represented by two monomers while connected monomers will have distance $|\vec{n}| = 3.8 \mathring{A}$. Therefore, all resulting measures will be directly interpretable in \mathring{A} units.

The positions for each amino acid *i* to be fitted, i.e. the C_{α} position of the backbone P_i^b , and the centroid P_i^s (geometric center) of all non-hydrogen atom co-ordinates of the side chain, are extracted from the PDB file.

The lattice model is derived by one of the following procedures optimising either a distance or coordinate RMSD. Both methods are introduced for lattice proteins including side chains but can be used to derive backbone-only lattice models as well. A sketch of the fitting workflow is given in Fig. 1.

dRMSD Optimisation

The fitting follows a greedy iterative chain-growth procedure. The initial lattice model's backbone and side chain position $(M_1^b \text{ and } M_1^s)$ are placed arbitrarily but adjacent $(M_1^b - M_1^s \in N)$. For each iteration $1 < i \leq l$, all valid placements of the next M_i^b and M_i^s on the lattice are calculated. A distance RMSD (dRMSD, Eqn. 1) evaluation is used to identify the best n_{keep} structures of length *i* for the next extension iteration. Since dRMSD is a rotation/reflection independent measure, symmetric structures must be filtered.

To calculate the final fit of the initial protein P, a superpositioning of the dRMSD-optimised structure M and a reflected version M' is done using the method by Kabsch [36]. The superpositioning translates and rotates M/M' in order to achieve the best mapping onto P. The superpositioning with lowest co-ordinate RMSD (cRMSD, Eqn. 2) is selected and finally returned.

$$dRMSD = \sqrt{\frac{\sum_{i < j} (|P_i - P_j| - |M_i - M_j|)^2}{l \cdot ((2 \cdot l) - 1)}}$$
(1)
with $P = P^s \cup P^b$, and $M = M^s \cup M^b$.
cRMSD = $\sqrt{\frac{\sum_{i=1}^l (|P_i^b - M_i^b|)^2 + (|P_i^s - M_i^s|)^2}{2 \cdot l}}$ (2)

cRMSD Optimisation

A cRMSD evaluation according to Eq. 2 depends on the superpositioning of the protein and its model. Thus the best relative lattice orientation has to be identified in addition to the best model. Once the orientation is fixed, a cRMSD evaluation allows for a fast, additive RMSD update along the chain extension.

We implement a cRMSD optimising method following [6, 17] as an alternative fitting strategy. In general a user defined number of rotation intervals rare performed for each of the XYZ rotation axes. For each rotation, we transform P^b and P^s into \hat{P}^b and \hat{P}^s , respectively, to obtain the rotated current target structure.

The fitting procedure follows a chain-growth approach: P_1^b is placed onto an arbitrary lattice node M_1^b and P_1^s to the closest representative node M_1^s adjacent to M_1^b . Now, all valid placements of the next M_i^b and M_i^s on the lattice are calculated. Using the co-ordinate RMSD (cRMSD, Eqn. 2) we evaluate all

derived models and keep the best n_{keep} for the next extension following [17] until all amino acids have been placed.

By applying the above cRMSD based fitting procedure we obtain the best fit for the current rotation. An iterative application of this procedure then results in the overall best fit for all screened rotations. Since our screen of XYZ rotations was discretised, the current rotation might be refineable. Therefore, another rotational refinement can be applied that investigates r^{ref} small rotation intervals around the best rotation from the first screen [6].

The run time of the cRMSD-method scales with respect to the lattice co-ordination number, n_{keep} , and most importantly the number of rotation intervals r and r^{ref} considered.

Futher Features

Coordinate data in the PDB is often incomplete. For example flexible loop structures are hard to resolve by current methods [37]. This results in missing coordinate data for certain substructures within PDB files. LatFit enables a structural fitting of even such fragmented PDB structures. It produces a lattice protein fragment for each fragment of the original protein while ensuring that all are placed in the same lattice orientation.

Currently, LatFit supports the 2D-square, 3Dcubic (100), 3D face centered cubic (FCC, 110) and 3D knights walk (210) lattice. The modular software design of our open source program enables an easy and straight forward implementation of other lattices.

Supported output formats of LatFit are the PDB format, the Chemical Markup Language (CML) format, as well as a simple XYZ coordinate output. A highly compact string representation of the lattice protein is also given in absolute move strings that encode the series of neighboring vectors $\vec{n} \in N$ along the structure.

The generated absolute move string can be directly used to apply other lattice protein tools onto the resulting structures, e.g. from the CPSPpackage for HP-type lattice protein models [10, 38] or from the LatPack tools for arbitrary lattice models [11, 39].

The web interface of LatFit, integrated into the CPSP-web-tools [38], enables *ad hoc* usage of the tool. Either a protein structure in PDB format can be uploaded or a valid identifier from the PDB database

given.

Our default parameters enable a direct application of LatFit resulting in a balanced tradeoff between runtime and fitting quality. The computations are done remotely on a computation cluster while the user can trace the processing status via the provided job identifier and according link. Results are available and stored for 30 days.

Results can be visualised using Jmol [40] for an interactive presentation of the final protein structure. The output file is also available for download. The final dRMSD and cRMSD values of the lattice protein compared to the original protein are given as well as the absolute move string encoding of the resulting structure. For an example of the LatFit web interface see Fig. 2.

Further details regarding the methods implemented, the output formats supported and the applicable parameterisation are located in the LatFit manual distributed with the source code. We provide an extensive help page and a frequently asked questions (FAQ) section within the web interface.

http://www.bioinf.uni-freiburg.de/Software/LatPack/

A web interface for *ad hoc* usage is available at

http://cpsp.informatik.uni-freiburg.de

Results and Discussion

We use LatFit to derive protein models on the commonly used 3D cubic, FCC, and knights walk lattices [17]. Our test set was taken from the PISCES webserver [41] on March 10^{th} 2009 (40% sequence identity cut-off, chain length 50-300, R-factor ≤ 0.3 and resolution $\leq 1.5 \text{\AA}$). Given our requirement for side chains, C_{α} -only chains were ignored. The resulting benchmark set contains 1198 proteins exhibiting a mean length of 160 ($\sigma = 64$).

In accordance with previous studies [17], cRMSD and dRMSD are used to assess model quality. cRMSD measures the similarity in co-ordinate position whereas dRMSD measures the similarity of interatomic distances. Due to the scaling of our lattice, RMSD results are in \mathring{A} rather than the scaled values provided by Ponty et al. [21].

Each protein was fitted twice onto the lattice using either our dRMSD or cRMSD-optimising method. dRMSD-optimisation was parameterised with $n_{keep} = 1000$. For cRMSD-optimising runs, we used the parameters r = 10 and $r^{ref} = 5$ for backbone-only fits, and r = 5 and $r^{ref} = 3$ for side chain fits. A rotation range of $[0, \frac{\pi}{2}]$ and $n_{keep} = 5$ was used for initial rotations. Rotational refinement was applied onto the interval $\pm [0, \frac{\pi}{10}]$ around the best initial rotation to derive the final fit.

Our backbone model RMSD values presented in Table 1 are competitive or superior to known fitting results from the literature [6, 12, 17] and reproduce the high quality previously achieved by other methods using the FCC and 210 lattices.

LatFit is designed for side chain models and results here are strong (see Table 2). In general, side chain models produce slightly larger RMSD values than the equivalent backbone model. This is due to the fact that the variation in distance between consecutive C_{α} atoms (fitted in both models) is lower than that between C_{α} atoms and their side chain centroid (fitted only in side chain models). In lattice models every distance is fixed at 3.8A which results in a higher mean displacement of the side chain. Nevertheless, high accuracy fits are still attained. Results in our test set have mean dRMSDs of about 1.5 and 1.2Å in the FCC and 210 lattice respectively. The strength of LatFit is its ability to produce both side chain and backbone-only lattice protein models. High accuracy models can be produced on the FCC lattice in seconds to minutes. Fits on the 210 lattice take orders of magnitude longer for relatively little gain in model accuracy. For this reason we recommend using the FCC lattice for detailed high-throughput protein structure studies in both backbone-only and side chain representing lattice models.

Conclusion

LatFit enables the automated high resolution fitting of both backbone and side chain lattice protein models from full atomic data in PDB format. We demonstrate its high accuracy on three widely used lattices using a large, non-redundant protein data set of high resolution. Side chain fits show on average a higher deviation than backbone models, but both produce high quality fits with results generally less than 1.5Å on the face-centred cubic lattice. To our knowledge, this is the first study and publicly available implementation for side chain models in this field. Available via web interface and as a stand-alone tool, LatFit addresses the lack of available programs and is well placed to enable further, more detailed investigation of protein structure in a reduced complexity environment.

Availability and Requirements

Project name: LatFit

Project home page: Web interface and source at http://cpsp.informatik.uni-freiburg.de

http://www.bioinf.uni-freiburg.de/Software/LatPack/

Operating system(s): Web interface: all common browser supporting Javascript and Java applets (for visualisation); Source: all Linux based systems (including Cygwin for MS WindowsTM)

Programming language: Web interface: Java Server Pages (JSP) and Javascript; Source: C++

Other requirements: BIU C++ library is part of the source package.

License: BSD-style license

Any restrictions to use by non-academics: none

Authors contributions

Idea and method design by MM, RS, and CD. Data set compiled by RS. Implementation and verification done by MM. CS and MM implemented the web interface. All authors contributed to and have approved the final manuscript.

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Figures

Figure 1 - Fitting workflow

The diagram depicts the the fitting process of LatFit for side chain models. Original full atom data is given in green, derived coordinates to fit in blue, and the lattice protein model in orange.



Figure 2 - LatFit web interface

A screenshot of the LatFit web interface result visualisation.





Tables

Table 1 - Method evaluation for backbone-only models

The table compares the RMSD mean values (μ) and standard deviations (σ) from literature to the results from our LatFit cRMSD-optimisation methods for *backbone-only models* on three different lattices.

	Results taken from		Results taken from	LatFit	
	Park and Levitt [17]		Ponty et al. [21]	cRMSD optimisation	
	dRMSD	cRMSD	cRMSD	dRMSD	cRMSD
	μ	μ	μ (rescaled to \mathring{A})	μ / σ	μ / σ
cub	2.34	2.84	$3.5 \ (0.923 \cdot 3.8)$	2.042 / 0.228	2.539 / 0.234
fcc	1.46	1.78	-	1.319 / 0.086	$1.641 \ / \ 0.090$
210	1.02	1.24	-	0.931 / 0.060	$1.154 \ / \ 0.060$

Table 2 - Method evaluation for side chain models

The table gives the RMSD mean values (μ) and standard deviations (σ) of the results from our dRMSDand the cRMSD-optimisation methods for *side chain models* on three different lattices.

	LatFit - dRM	SD optimisation	LatFit - cRMSD optimisation		
	dRMSD	cRMSD	dRMSD	m cRMSD	
	μ / σ	μ / σ	μ / σ	μ / σ	
cub	2.779 / 0.754	4.157 / 1.331	2.609 / 0.481	3.286 / 0.624	
\mathbf{fcc}	$1.496 \ / \ 0.153$	2.104 / 0.246	1.495 / 0.061	1.839 / 0.068	
210	$1.126 \ / \ 0.068$	$1.601 \ / \ 0.100$	$1.185 \ / \ 0.042$	$1.450 \ / \ 0.047$	